## Maths for Computing Tutorial 13

1. Construct the DFAs for the following languages over $\{0,1\}$ :
a) $L=\{w \mid w$ contains at least two 1 s$\}$.
b) $L=\left\{w \mid\right.$ for every prefix $x$ of $\left.w,\left|\#_{0}(x)-\#_{1}(x)\right| \leq 2\right\}$. $\left(\#_{0}(x)\right.$ denotes the number of $\left.0 \sin x\right)$.
c) $L=\{w \mid$ decimal representation of $\operatorname{reverse}(w)$ is a multiple of 3$\}$.
2. Prove that the following languages over $\{0,1\}$ are non-regular.
a) $L=\left\{w w \mid w \in\{0,1\}^{*}\right\}$.
b) $L=\left\{w \mid w=1^{k} z\right.$ where $z$ contains at most $k$ many 1 s $\}$.
c) $L=\left\{0^{n} \mid n\right.$ is a prime number $\}$.
3. Prove or disprove that the following language over $\{0,1\}$ is regular:
$L=\left\{w \mid w=u v\right.$ where $\left.\#_{0}(u)=\#_{1}(v)\right\}$
4. Construct CFGs for the following languages over $\{0,1\}$ :
a) $L=\{w \mid w$ contains equal number of 0 s and 1 s$\}$.
b) $L=\left\{w \mid w\right.$ is not of the form $\left.0^{n} 1^{n}\right\}$.
